



# Ionospheric heating effects on transionospheric VLF to MF propagation

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DEMETER 2011 Workshop

DEMETER observations have raised questions on the propagation of plasma waves through the ionosphere

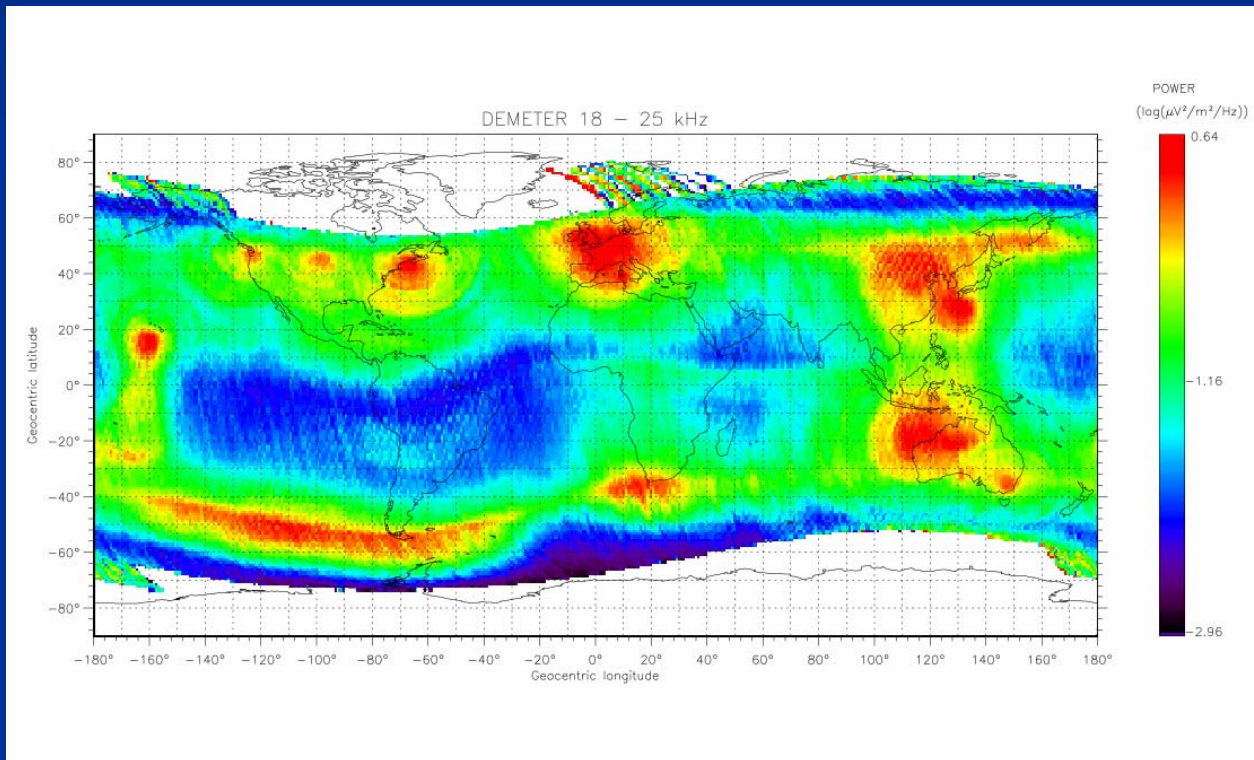
Preliminary answers have been given in Parrot et al. 2008 and 2009 papers

The aim of the present paper is to provide a general view on :

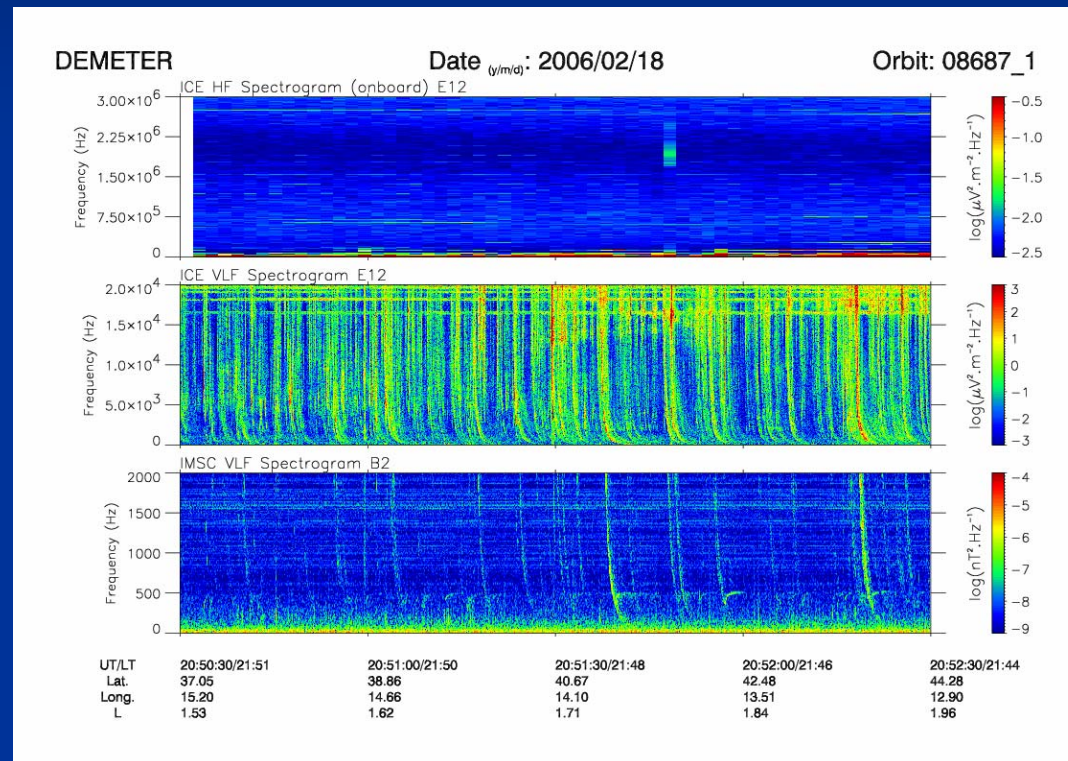
**Propagation of cold plasma waves**

# 1. Questions raised by DEMETER

**QUESTION 1 - Dispersion of nighttime VLF signals (18-25 kHz), recorded from 2006 to 2008, above powerful VLF transmitters (Parrot et al., JGR, Vol 114, 2009) ?**



## QUESTION 2 -Origin of bursts of MF bands ( $\sim 2. - 2.5$ MHz) in geographical regions far from VLF transmitters ( Parrot et al. , JGR, Vol. 113, 2008) ?

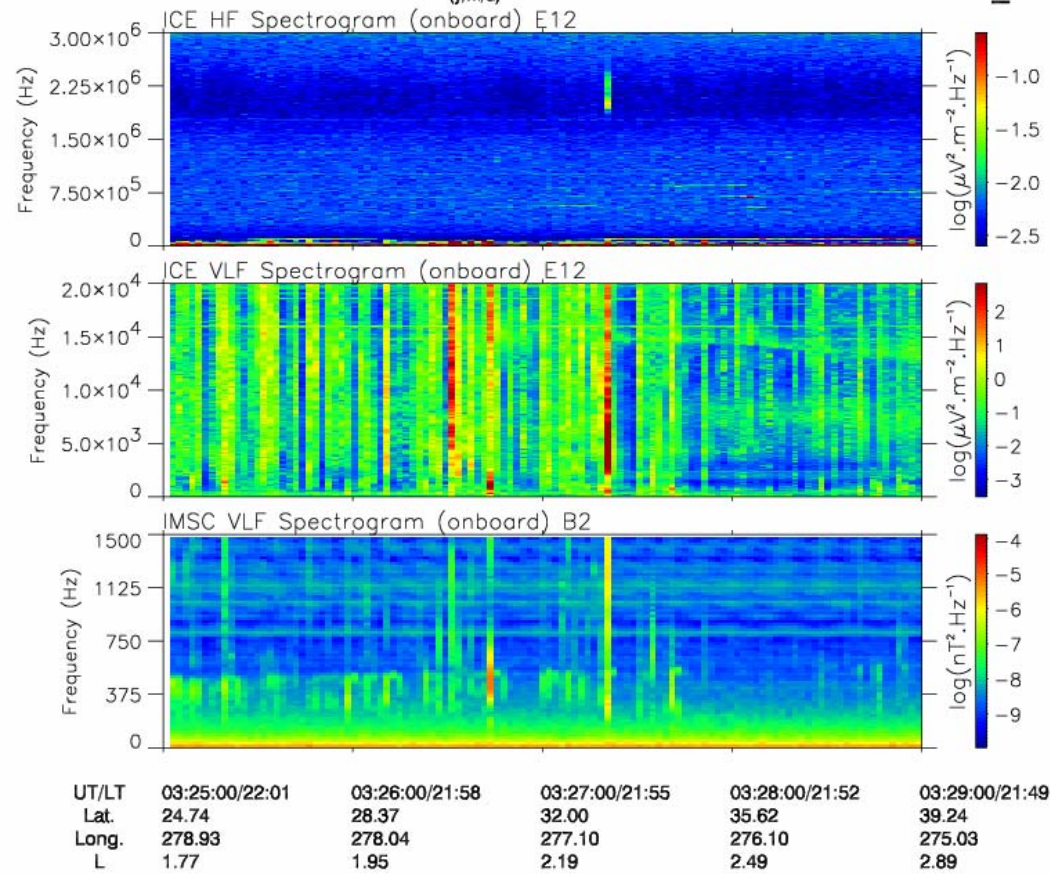


The peaks in intensity correspond to intense 0+ whistlers

DEMETER

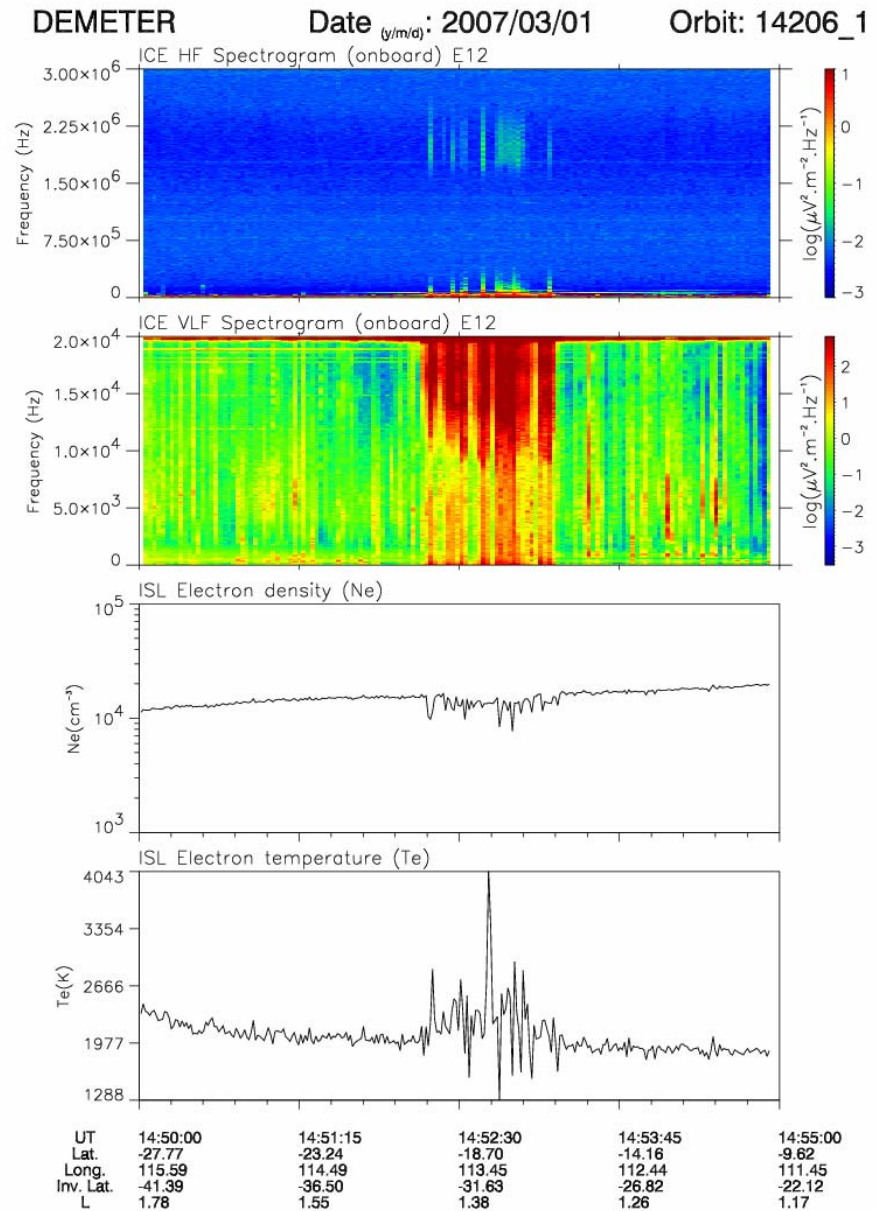
Date <sub>(y/m/d)</sub>: 2006/01/31

Orbit: 08412\_1

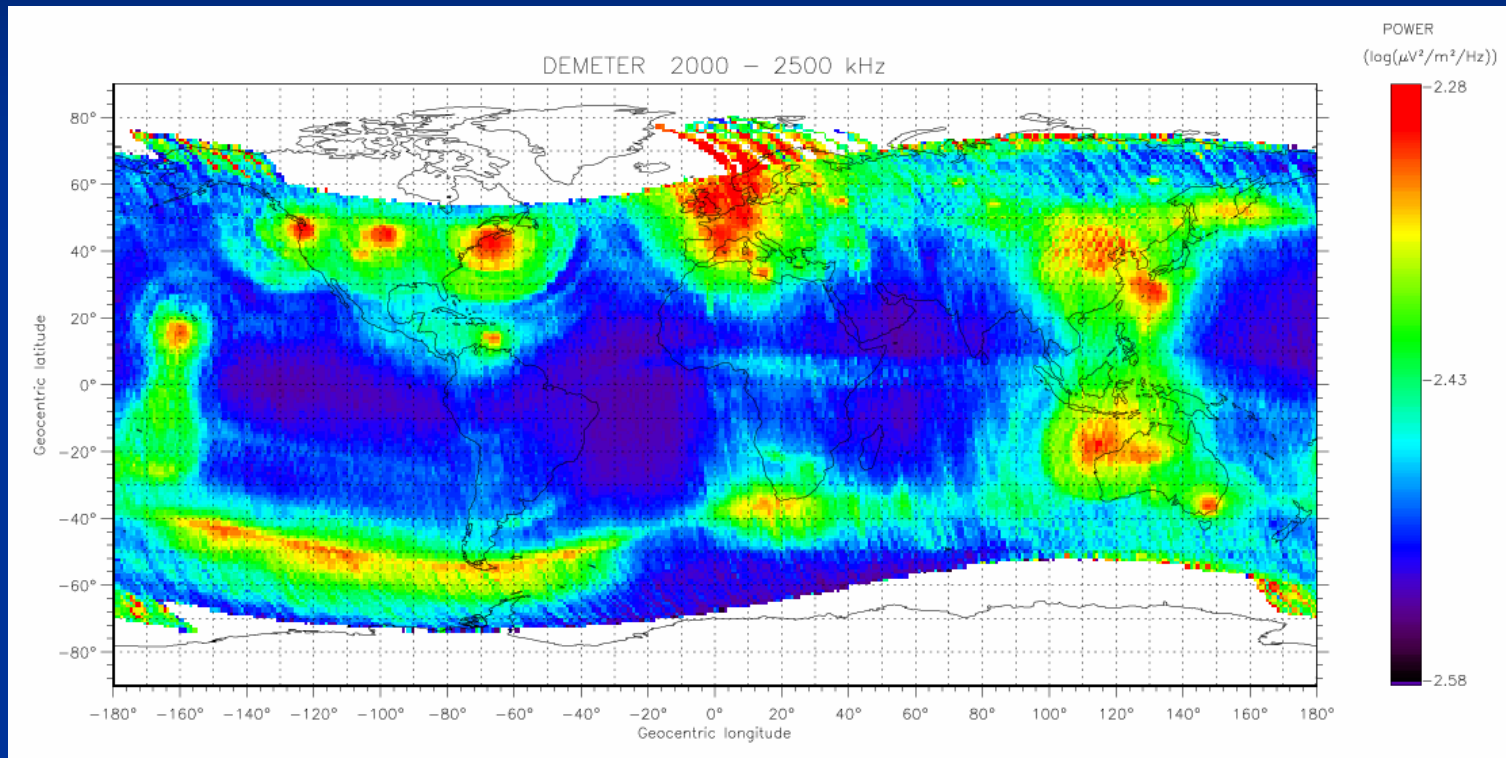


**QUESTION 3 - Origin of  
MF bands ( $\sim 2. - 2.5$  MHz)  
above the NWC transmitter  
( Parrot et al. , JGR, Vol. 114,  
2009) ?**

**Propagation through  
density irregularities?**



## QUESTION 4 - Origin of nighttime MF signals (2 – 2.5 MHz), recorded from 2006 to 2008, above powerful VLF transmitters (Parrot et al., JGR, Vol 114, 2009) ?



The peaks in intensity correspond to  $\sim 3\text{dB}$  enhancements of the lightnings above powerful VLF transmitters

Propagation through density irregularities?

Answers will be looked for from variations in the refractive index  $n^2$  (Appleton – Lassen formula)

$$n^2 = 1 - \frac{A(X,U)}{B(X,Y,\theta,U) \pm \{C(X,Y,\theta,U)\}^{1/2}}$$

$$X = f_{pe}^2 / f^2$$

$$Y = f_{ce} / f$$

$$\theta = (k, B_0)$$

$$U = 1 - iZ \text{ with } Z = \nu / \omega \text{ } (\nu, \text{ collision frequency})$$

Ordinary wave  
+ sign for  $\pm \{ \}^{1/2}$

Extraordinary wave  
- sign for  $\pm \{ \}^{1/2}$

## Cold and collisionless plasma waves

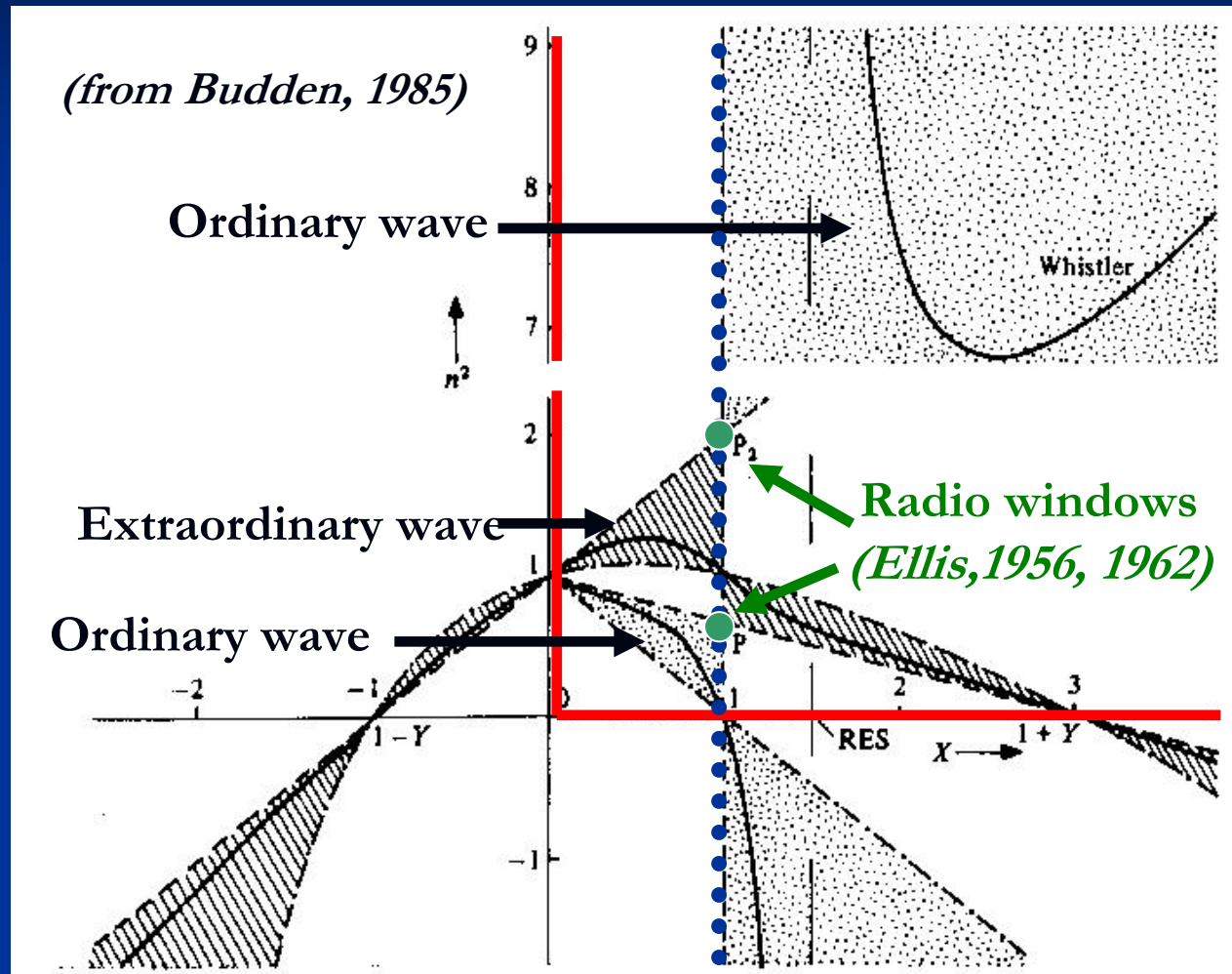
$$Y = f_{ce}/f > 1$$

(ELF, **VL**F, LF, lower part of MF)

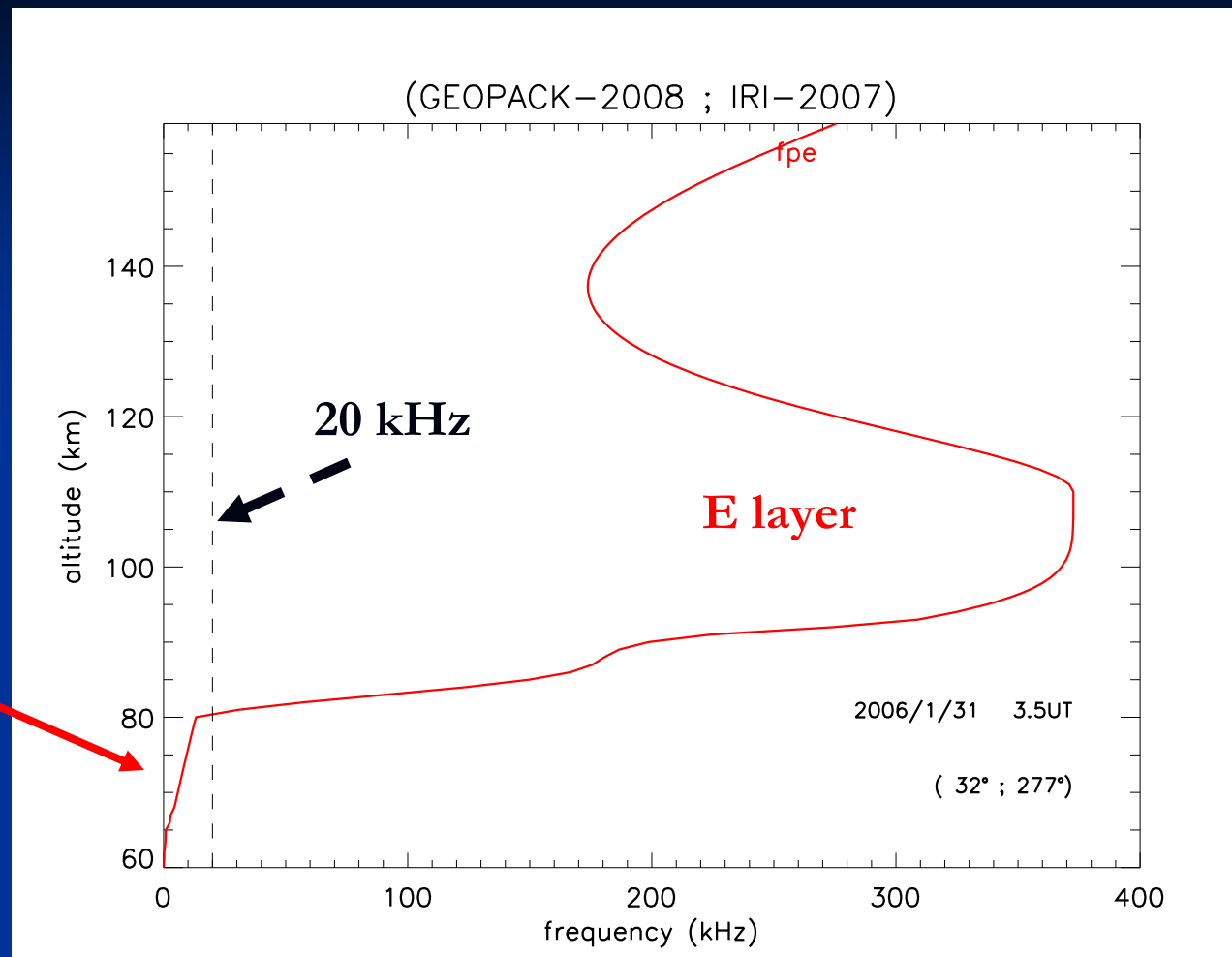
$$U=1$$

Two windows points:

- P, propagation stopped for  $X = 1+Y$
- P<sub>2</sub>, propagation to space



Extrapolation  
for altitudes  
below 80 km



$f = 20 \text{ kHz}$

$\nu < 5.82 \cdot 10^3 \text{ s}^{-1}$  at 85 km altitude

$h < 80 \text{ km}$ , Ex Mode

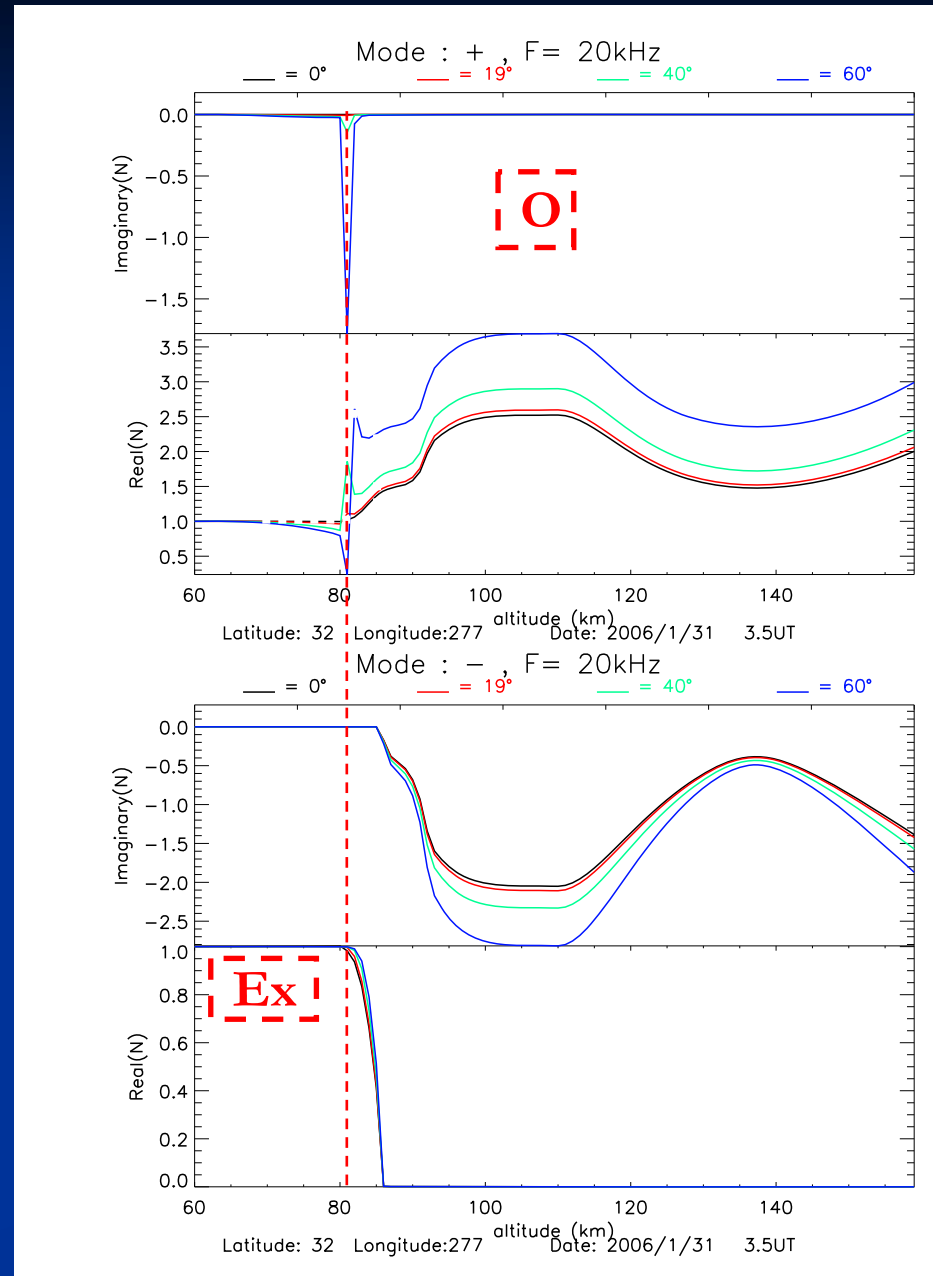
1<sup>st</sup>  $X = 1$  crossing, Ex  $\rightarrow$  O mode

$\theta = 0^\circ$  crosses  $X = 1$

propagation up to 2d crossing (if any)

For all other  $\theta$  values, discontinuity and absorption around  $X = 1$   
(if generated at altitudes where  $X > 1$ , they may propagate)

*O waves generated below  $X = 1$  are transmitted in Ex mode then are stopped at the altitude where  $X = 1 + Y$*

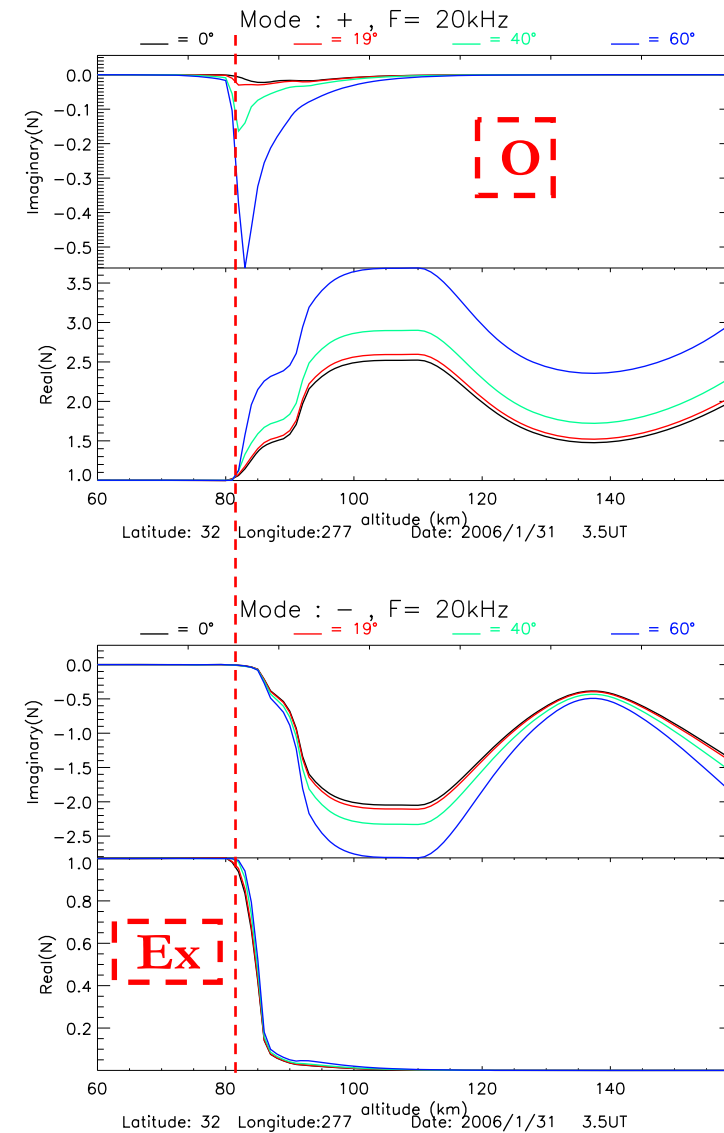


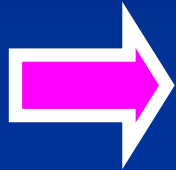
For  $\sim \nu = 5.82 \cdot 10^5 \text{ s}^{-1}$   
at 85 km altitude

all the oblique waves  
cross the  $X = 1$  cut-off

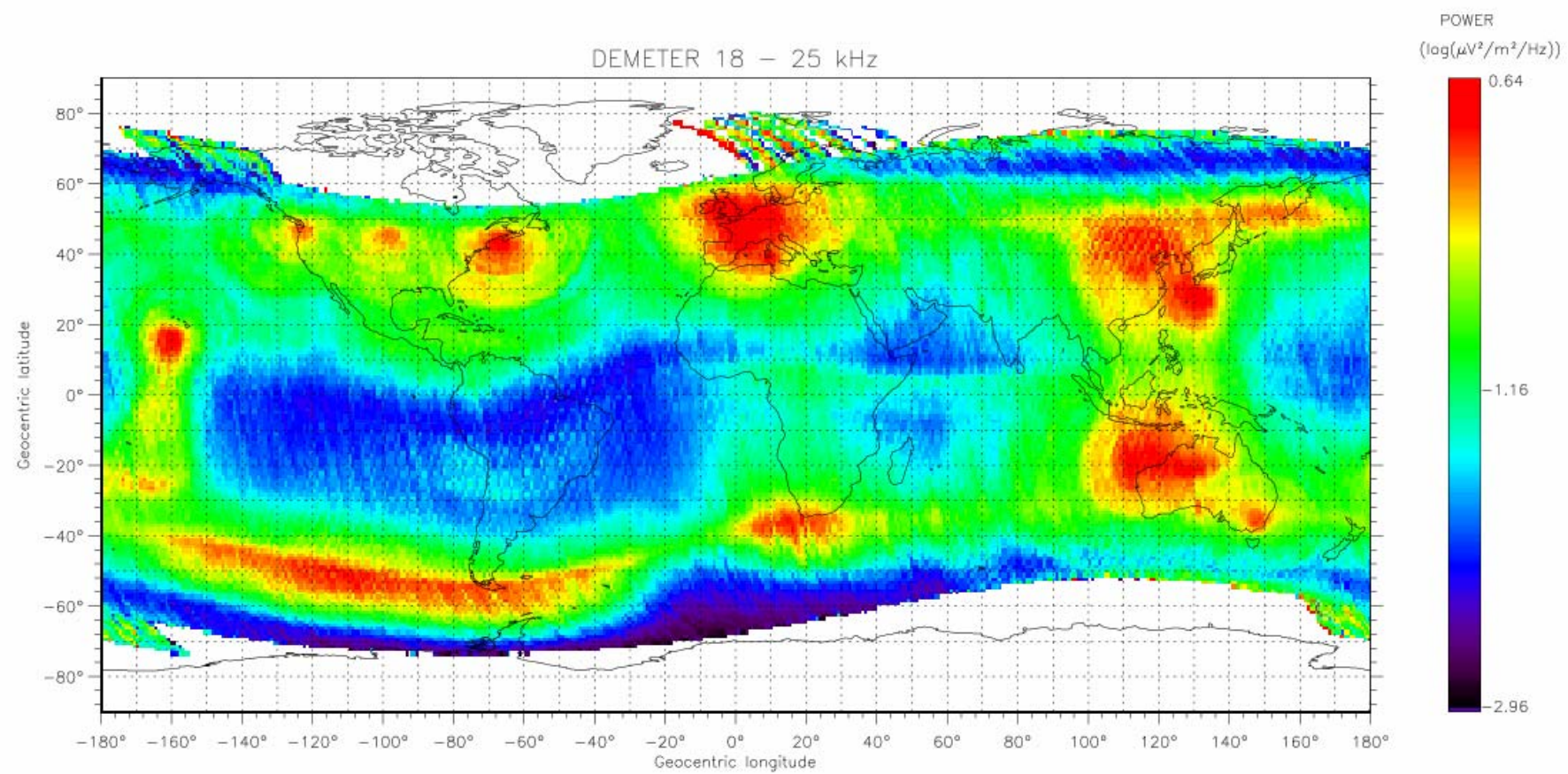
Globally, the attenuation  
factor has been reduced.

The VLF observations are  
more geographically  
dispersed above powerful  
transmitters





- Heating produced by powerful VLF transmitters increase the electron collision frequency
- Increases in the electron collision frequency affect the transparency and the angular width of the radio windows
- This answers question 1 (see next slide)



## Cold and collisionless plasma waves

$$Y = f_{ce}/f < 1$$

(higher part of MF waves)

$U=1$

The only waves which reach the DEMETER altitude are those generated in the O mode at altitudes below  $X = 1$ , then propagated in the Extraordinary mode with

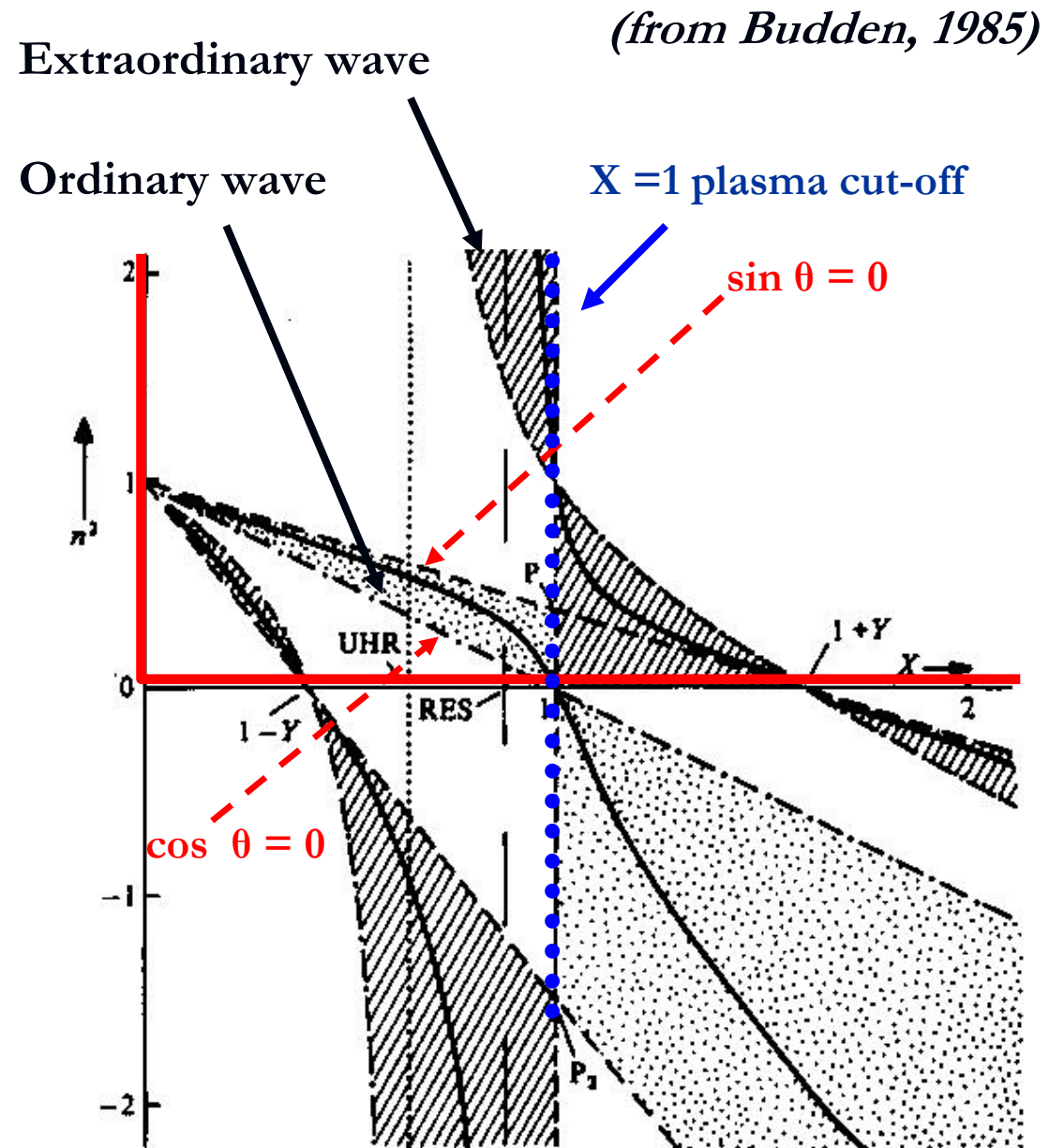
$$X < 1+Y$$

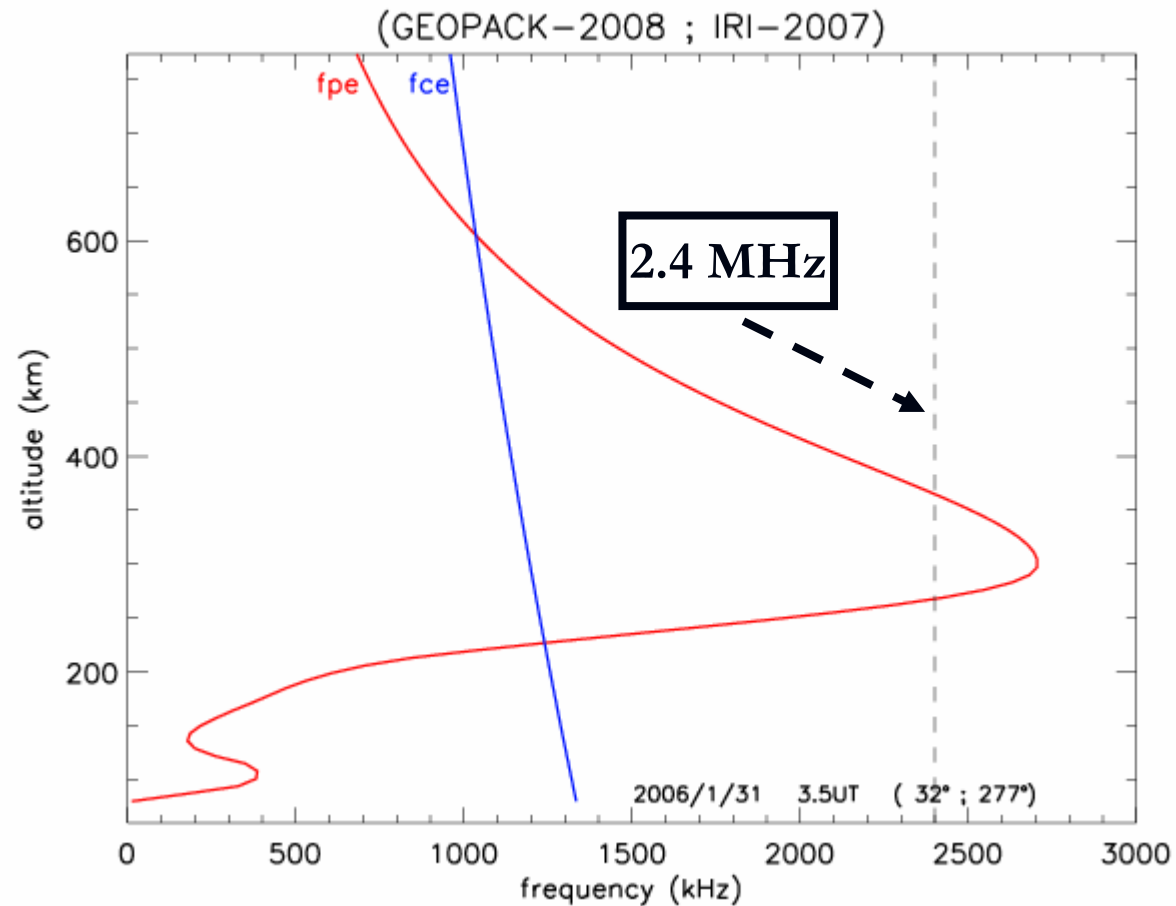
i.e.

$$f_p^2/f^2 < 1 + f_{ce}/f$$

or

$$f_p^2 < f(f + f_c)$$





Condition for crossing the F layer :  $f_p^2 < f(f + f_{ce})$

- at the max of the F layer,  $f_{ce} \sim 1.2$  MHz
- for  $f = 2.4$  MHz,  $f_p$  must be  $< 2.94$  MHz



the 2.4 MHz wave crosses the ionosphere

$f = 2400 \text{ kHz}$ ,  $Y < 1$

$h < 250 \text{ km}$ , O Mode

all waves may propagate

1<sup>st</sup> X = 1 crossing

$\theta = 0^\circ$  crosses X = 1  
propagation up to 2<sup>d</sup> crossing

$\theta = 19^\circ$  crosses X = 1  
stops before 2<sup>d</sup> crossing

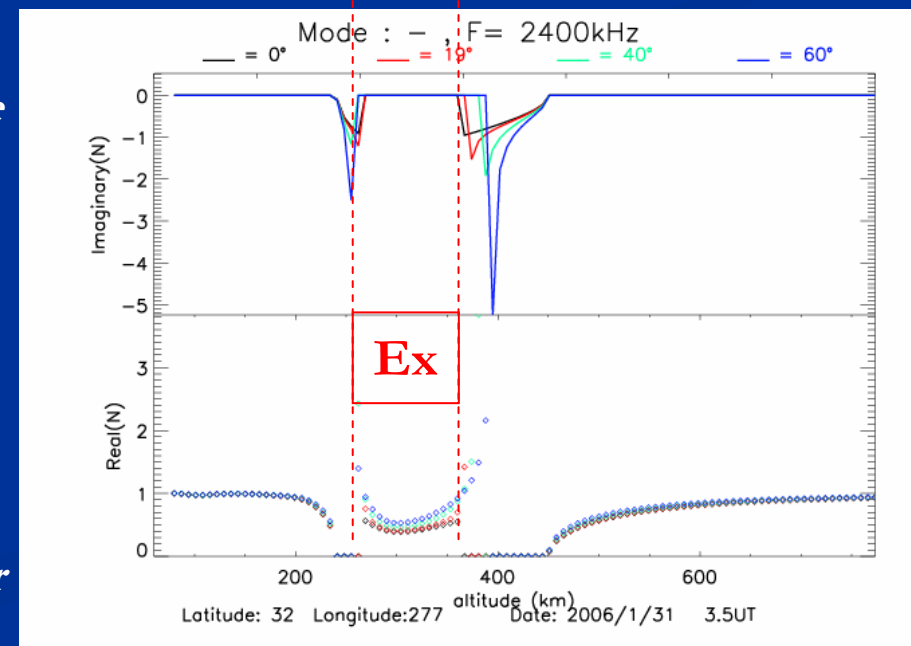
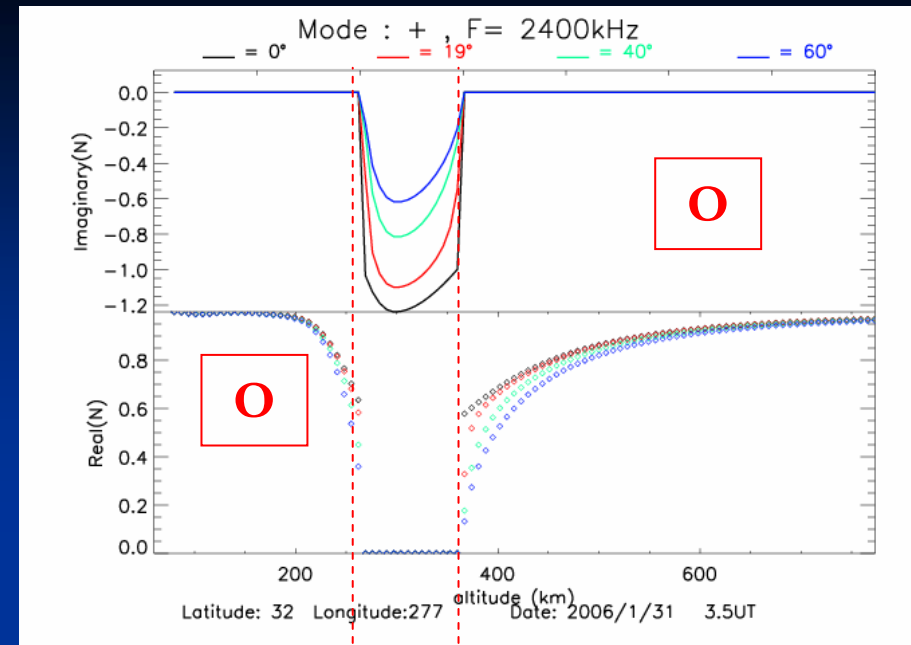
$\theta = 40^\circ$  does not cross X = 1  
(if generated there, may propagate  
between ~ 250 to 410 km)

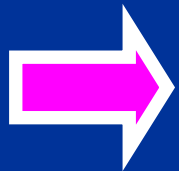
$\theta = 60^\circ$  does not propagate

2<sup>d</sup> crossing

$\theta = 0^\circ$  crosses X = 1  
then propagates to space

*Above 2<sup>d</sup> crossing, if generated there, other  
 $\theta$  values may propagate.*





■ Far from powerful VLF transmitters, the MF waves that are observed on DEMETER respect the condition  $X < 1+Y$  all over their propagation path (the F layer maximum plasma frequency is generally rather low).

■ The upper cut-off of the MF band seems to be due to :

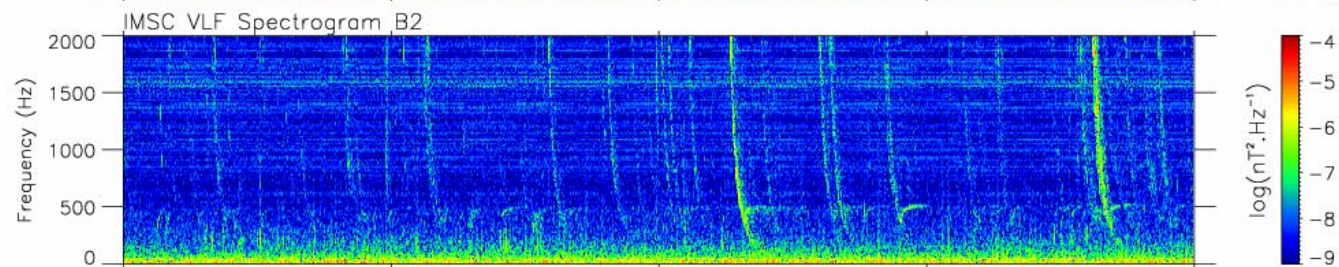
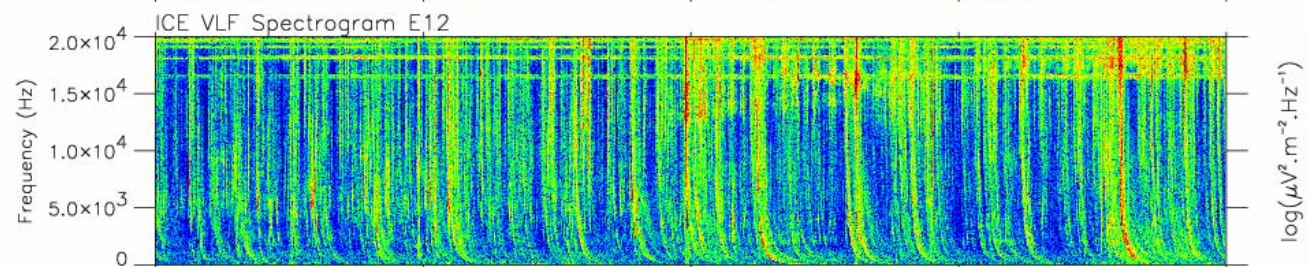
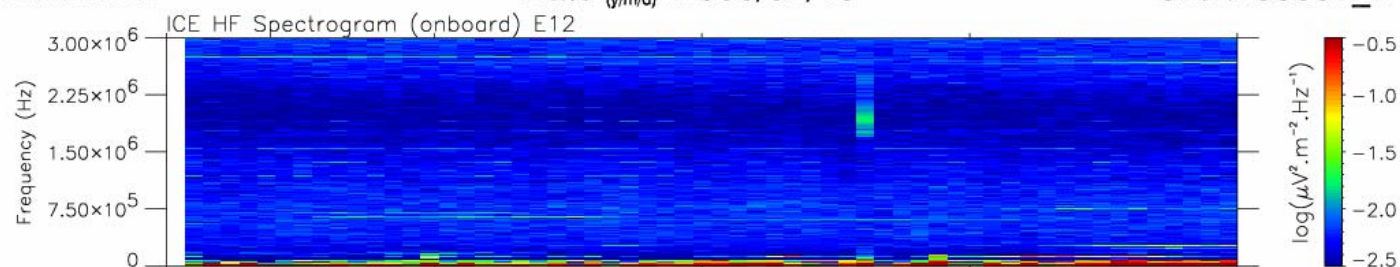
- the slope of the power spectrum of the observed  $O^+$  whistlers
- or/and the slope of the filters used for the HF electric field measurements

■ This answers question 2 (see next slide)

# DEMETER

Date (y/m/d): 2006/02/18

Orbit: 08687\_1

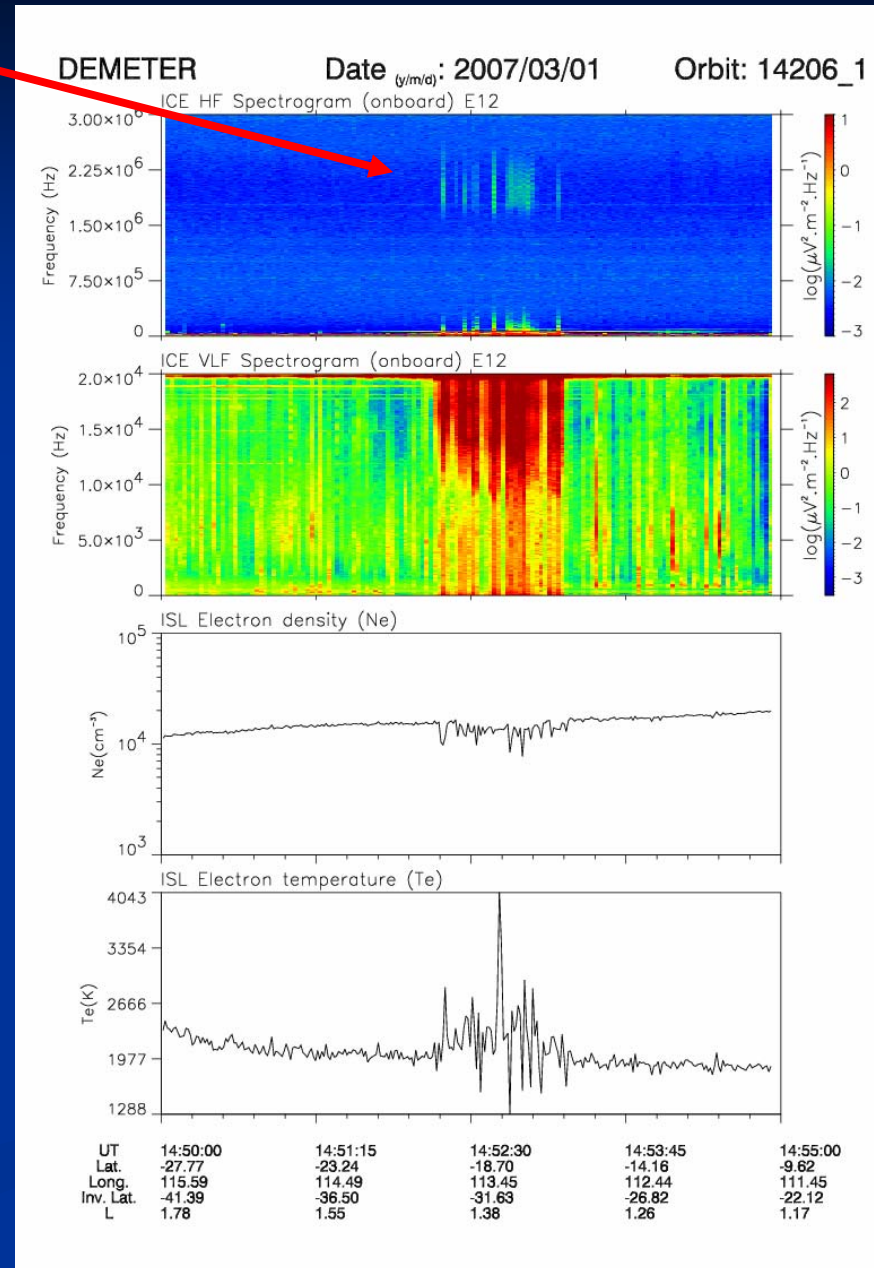


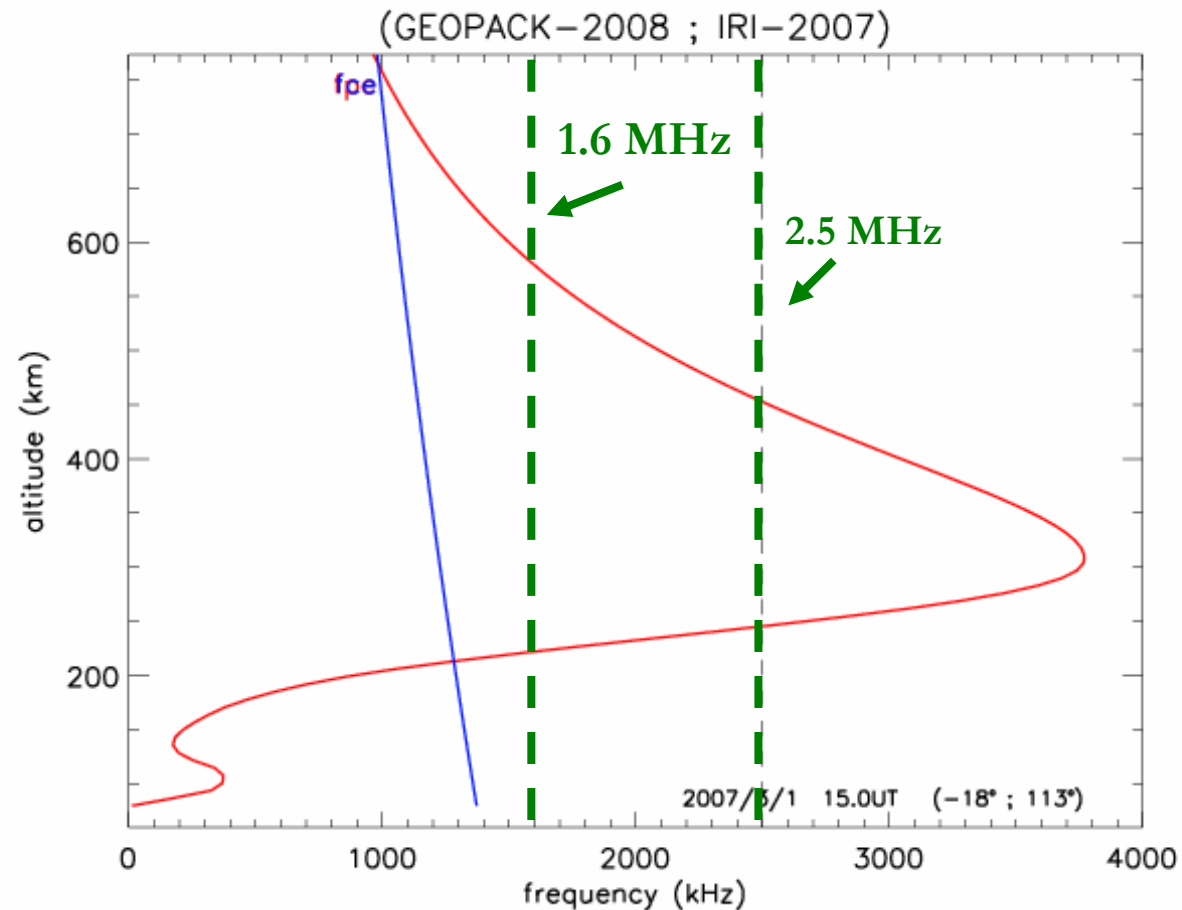
|       |                |                |                |                |                |
|-------|----------------|----------------|----------------|----------------|----------------|
| UT/LT | 20:50:30/21:51 | 20:51:00/21:50 | 20:51:30/21:48 | 20:52:00/21:46 | 20:52:30/21:44 |
| Lat.  | 37.05          | 38.86          | 40.67          | 42.48          | 44.28          |
| Long. | 15.20          | 14.66          | 14.10          | 13.51          | 12.90          |
| L     | 1.53           | 1.62           | 1.71           | 1.84           | 1.96           |

1.6 – 2.5 MHz  
frequency band

Other interpretations are  
needed when the F layer  
maximum  $f_p$  value is too large  
to respect  $X < 1+Y$

i.e. if plasma waves  
propagation laws don't apply





Condition for crossing the F layer :  $f_p^2 < f(f + f_{ce})$

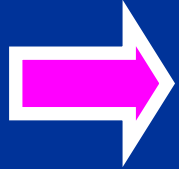
- at the max of the F layer,  $f_{ce} \sim 1.2$  MHz
- for  $f = 2.5$  MHz,  $f_p$  must be  $< 3.04$  MHz
- for  $f = 1.6$  MHz,  $f_p$  must be  $< 2.09$  MHz



**No crossing of the MF band without density depletion**

## Possible interpretation:

- The 1.6 – 2.5 MHz frequency band observed on DEMETER requires a density depletion with a maximum  $f_p$  value  $< 2$  MHz
- density depletions may be associated with the Ne irregularities produced by the NWC VLF transmitter and observed on DEMETER (depletions of the order of  $\sim 50\%$ , lateral extension of the order of a few kms )
- those observations fit with the order of the density depletion required for the crossing of the F layer (depletions of the order of  $70\%$  around the maximum of the F layer) .

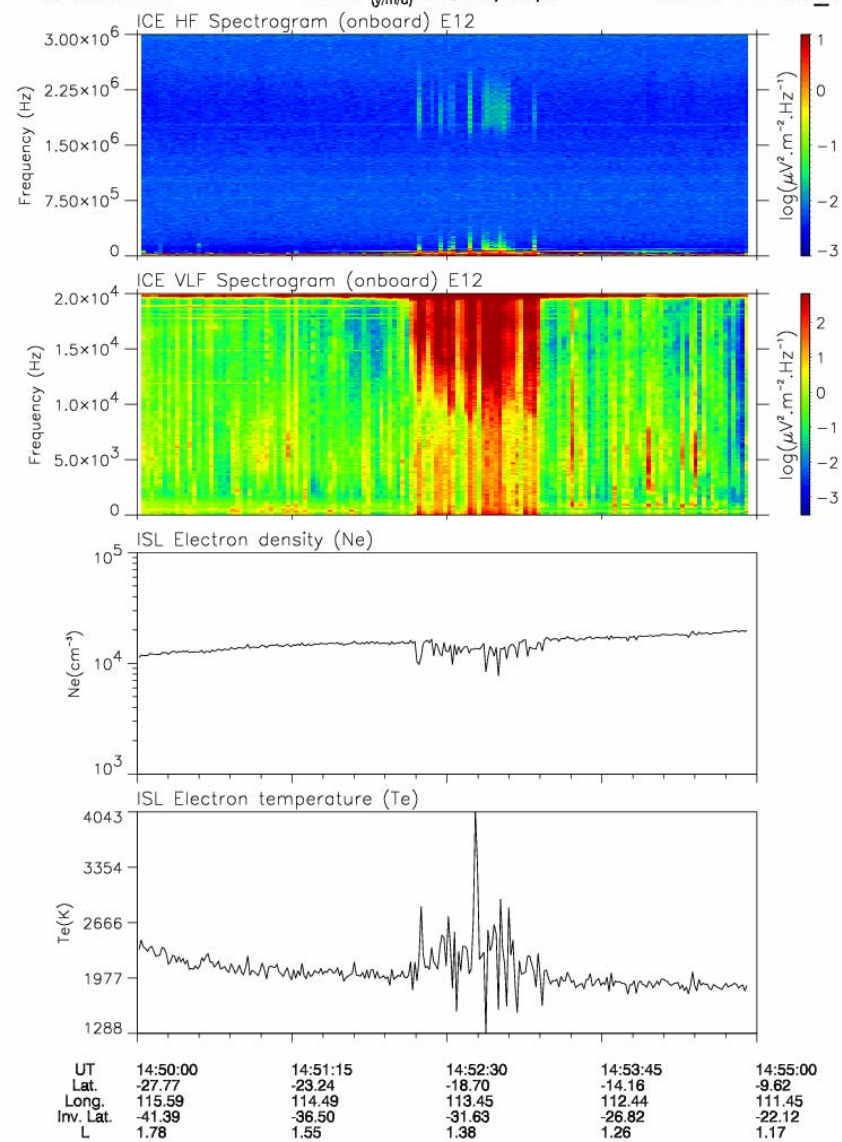


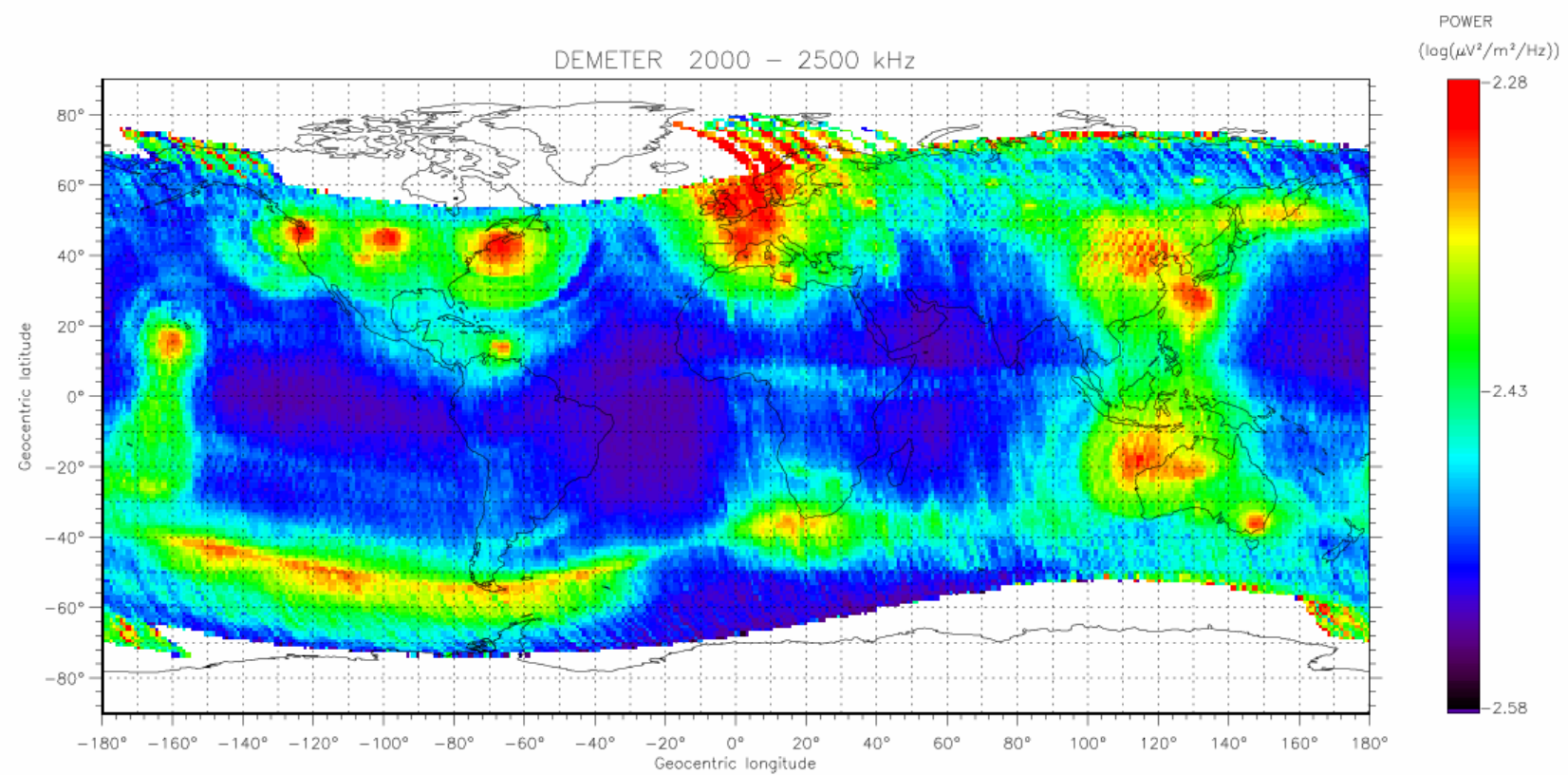
- Powerful VLF transmitters may generate density depletions allowing MF signals to cross the ionosphere.
- This answers questions 3 and 4 (see next two slides)

DEMETER

Date (y/m/d): 2007/03/01

Orbit: 14206\_1





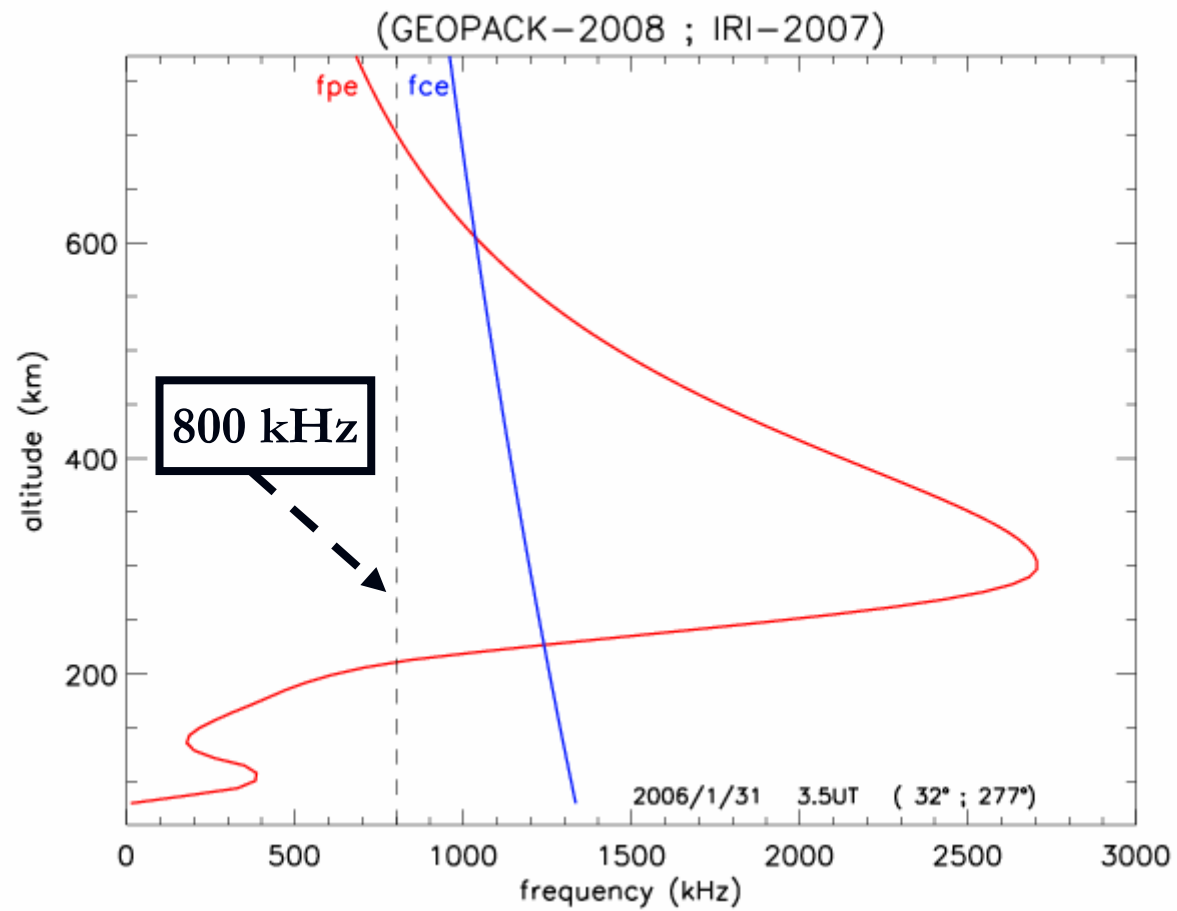
# CONCLUSION

## ■ Far from powerful VLF wave transmitters

The propagation laws of plasma waves (e.g. Budden, 1985) applies.  
They explain all original observations made by DEMETER

## ■ Above powerful VLF transmitters

- increases in the electron collision frequency, increase the angular width of the waves which cross the  $X=1$  plasma cut-off at the bottom of the ionosphere (which explains dispersion of VLF waves above powerful VLF transmitters)
- generation of Ne irregularities produce Ne depletions allowing MF waves to cross the ionosphere even for large  $(f_p)_{\max}$ .



$f = 800 \text{ kHz}$ ,  $Y > 1$

$h < 200 \text{ km}$ , Ex Mode  
all waves may propagate

1<sup>st</sup> X = 1 crossing, Ex  $\rightarrow$  O mode

$\theta = 0^\circ$  crosses X = 1  
propagates up to 2<sup>d</sup> crossing

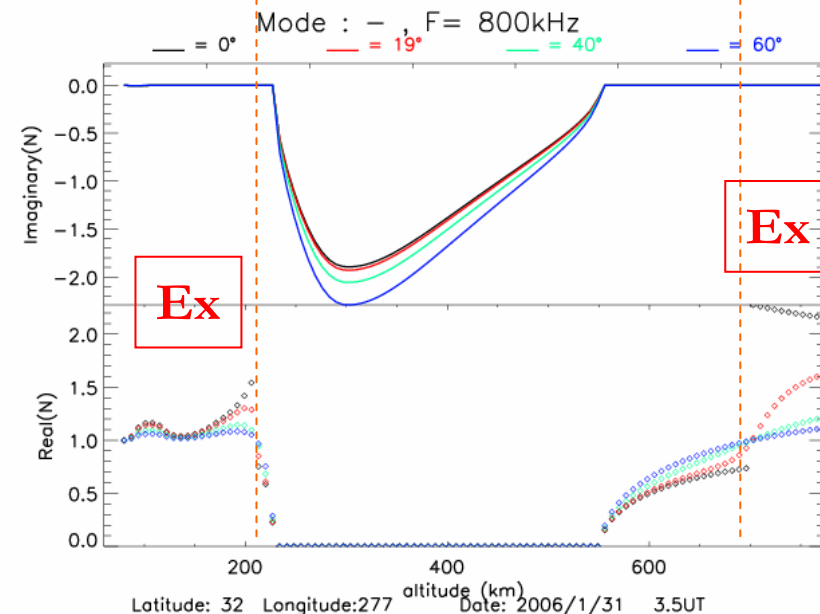
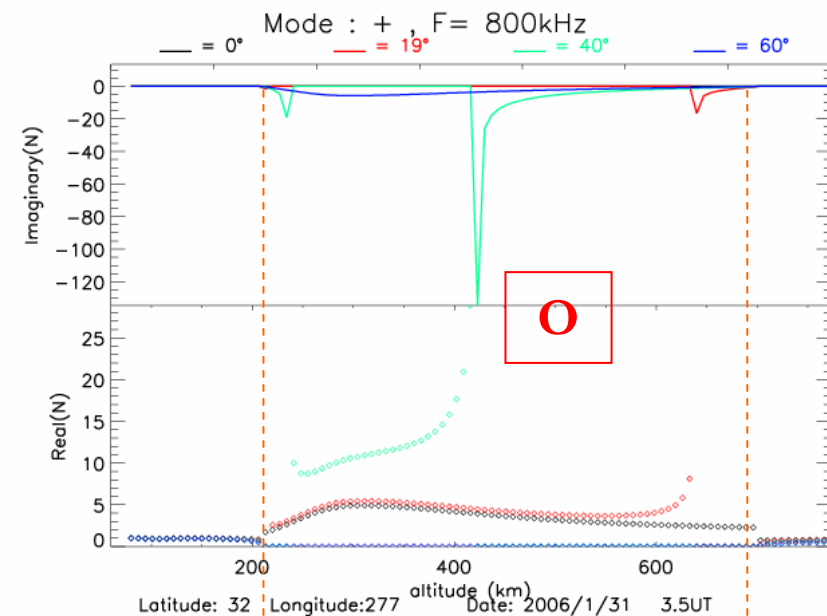
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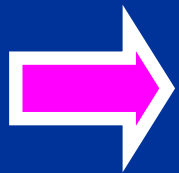
$\theta = 40^\circ$  does not cross X = 1  
if generated there, may propagate  
between  $\sim 250$  to  $410 \text{ km}$

$\theta = 60^\circ$  does not propagate

2<sup>d</sup> X=1 crossing, O  $\rightarrow$  E<sub>x</sub> mode

$\theta = 0^\circ$  propagates to space





According to their expected values at altitudes  $> 180$  km electron collision frequencies don't affect  $X = 1$  crossings.